May 31, 2022
The premise of the Poster is utility of a parametric solution curve definition for (index(0) of radicand(n). What happens when index solution curves operate on displacement integer(s) of Sir Isaac Newton captured as a radicand of square space math.

$$
(\sqrt[i n d e x]{\text { radicand }}) .
$$

## ALEXANDER; CEO SAND BOX GEOMETRY LLC

Central Force +domain integers and inversed exponents of curved 5/31/2022 5:04 AM space.

The meter of central force field cause and effect is called 'inverse square'. Essentially, we take a number line integer as displacement, change a central force interpretation of displacement from radius into an inversed denominator (curvature?). Then alter this meter of space into a degree2 curve analytics for cause and effect. This paper investigates discovery of Sir Isaac Newton's displacement radii behavior when

A study of displacement integer as radicand in central force field space: $\left(9^{\frac{1}{3}}\right),\left(9^{\frac{1}{2}}\right),\left(9^{\frac{1}{1}}\right),\left(9^{\frac{1}{0}}\right)$ captured as radicand (n) by indexed Parametric Solution Curve(s).
tune 14, 2022. 16 pages; 1600words. July 31, 2022. 19pages; 2100 words.

## ABSTRACT:

On the parametric geometry of inverse(d) exponents.
Exponents are a straightforward operation (number exponent). Roots have an alternate script and symbol. Given we know the $\left(3^{3}=27\right)$, we also recognize $(\sqrt[3]{27}=3)$. But not so often used is the written exponent for $(\sqrt[3]{27}) ;\left(27^{\frac{1}{3}}=3\right)$. There are three elements in the parametric geometry of roots: index; radical; and radicand. $\sqrt[i n d e x]{\text { radicand }}$.
We never include the index when writing square roots. The unused term for square root of 4 is: $(\sqrt[2]{4}=2)$. Or $\left(4^{\frac{1}{2}}\right)$.
We also have seldom seen exponents. $\quad\left(n^{0}=1\right) ;\left(n^{1}=n\right)$
Setting these exponents ( 0 and 1 ) as radical index:
$(\sqrt[1]{n})=n, \quad$ and $\quad(\sqrt[0]{n})=(1 / 0 \leftrightarrow$ indeterminate infinity encountered $)$.
This paper uses a GeoGebra parametric machine to find the $(\sqrt[0]{n})$, losing the (indeterminate infinity encountered) tag.

## Abstract history:

Abstract rejected for Contributed Paper; organizers recommend Contributed Poster Session.

Sponsor: Philosophy of Mathematics SIGMAA (POM-SIGMAA)
Organizers:
Jason Douma, University of Sioux Falls, jason.douma@usiouxfalls.edu
Tom Morley, Georgia Institute of Technology, Morley@math.gatech.edu

Players and reference: $(\sqrt[i n d e x]{\text { integer }})$. Let index be curved space Mechanical Energy causality. Let integer be metered displacement in field space. Let $\left(G * M_{1} * M_{2} *\left(\frac{1}{r}\right)^{2}\right)$ be cause and effect of G-field potential.

The Poster: Size is 3 ft by 4 ft . Here's the outline.
The top 1 foot will be a banner (page3) 4ft across.

## THE PARAMETRIC GEOMETRY of INVERSED EXPONENTS WORKING CENTRAL FORCE DOMAINS

$$
\text { Exploring: }\left(9^{\frac{1}{3}}\right),\left(9^{\frac{1}{2}}\right),\left(9^{\frac{1}{1}}\right),\left(9^{\frac{1}{0}}\right)
$$

PROBLEM: construct four parametric solution curves using inverse exponents.
Curved Space Parametric Solution: $\left(t, \frac{t^{\text {index }}}{\mp 2} \pm \frac{\text { radicand }}{2}\right)$.

## Confirm solution curve using Square Space Parametric Abscissa ID: $(\sqrt[i n d e x]{9}, t)$.

Readings from the Sand Box

The bottom 2 ft will be in 4 sections 1 ft across.

| Sect1 | Sect2 | Sect3 | Sect4 |
| :---: | :---: | :---: | :---: |
| $\left(9^{\frac{1}{3}}\right)$ | $\left(9^{\frac{1}{2}}\right)$ | $\left(9^{\frac{1}{1}}\right)$ | $\left(9^{\frac{1}{0}}\right)$ |

$\left(9^{\frac{1}{3}}\right)$, page (5-6)
$\left(9^{\frac{1}{2}}\right)$, page (7-8)
$\left(9^{\frac{1}{1}}\right)$, page (9-10)
$\left(9^{\frac{1}{0}}\right)$, page (11-12)

Parametric geometry construction for $(\sqrt[3]{9})$. ALIXAND $\quad$ R


Figure 1: parametric geometry $\left(9^{\frac{1}{3}}\right)$.

| Name | Value | Caption |
| :--- | :--- | :--- |
| Curve a | $(4.5 \cos (\mathrm{t}), 4.5 \sin (\mathrm{t}))$ | Independent curve (AKA discovery curve). |
| Curve b | $\left(\mathrm{t}, \mathrm{t}^{2} /-18+9 / 2\right)$ | Dependent curve (AKA definition curve). |
| Curve c | $(2.08, \mathrm{t})$ | abscissa definition $\sqrt[3]{9}$. |
| Curve d | $\left(\mathrm{t}, \mathrm{t}^{3} /-2+9 / 2\right)$ | $(-)$ solution curve. |

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Curve e ( \(\mathrm{t}, \mathrm{t}^{3} / 2-9 / 2\) ) ( + ) solution curve.
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Created with GeoGebra
odd indices:
> ( - ) solution ( $d$ ) comes from $Q 2$ infinity. Flat lines at $\mathbf{N}$ pole and finds $(\sqrt[3]{9})$ on accretion domain of $\left(M_{1}\right)$.

$(+)$ solution curve ( $e$ ) comes from $Q 3$ infinity. Flat lines at $\mathbf{S}$ pole and finds $(\sqrt[3]{9})$ on accretion domain of $\left(M_{1}\right)$.

Parametric geometry construction for $(\sqrt[2]{9})$. ALIXAND $\quad$ R


Figure 2: parametric geometry for $\left(9^{\frac{1}{2}}\right)$.

| Name | Value | Caption |
| :--- | :--- | :--- |
| Curve a | $(4.5 \cos (\mathrm{t}), 4.5 \sin (\mathrm{t}))$ | Independent curve (AKA discovery curve). |
| Curve b | $\left(\mathrm{t}, \mathrm{t}^{2} /-18+4.5\right)$ | Dependent curve (AKA definition curve). |
| Curve c | $(3, \mathrm{t})$ | Abscissa definition $(\sqrt[2]{9})$. |
| Curve d | $\left(\mathrm{t}, \mathrm{t}^{2} /-2+9 / 2\right)$ | $(-)$ solution curve. |

Curve e (t, $\left.\mathrm{t}^{2} / 2-9 / 2\right) \quad(+)$ solution curve.

Created with GeoGebra

## Parametric geometry construction for $(\sqrt[2]{9})$.

 even indices:( - ) solution (d) comes from $Q 3$ infinity. Flat lines at $\mathbf{N}$ pole and finds $(\sqrt[2]{9})$ on accretion domain of $\left(M_{1}\right)$.
$(+)$ solution curve ( $e$ ) comes from $Q 2$ infinity. Flat lines at $\mathbf{S}$ pole and finds $(\sqrt[2]{9})$ on accretion domain of $\left(M_{1}\right)$.

Parametric geometry construction for $(\sqrt[1]{9})$. ALIXAND $\quad$ R


Figure 3: parametric geometry ( $9 \frac{1}{1}$ ).

| Name | Value | Caption |
| :---: | :--- | :--- |
| Curve a | $(4.5 \cos (\mathrm{t}), 4.5 \sin (\mathrm{t})$ | Independent curve (AKA discovery curve). |
| Curve b | $\left(\mathrm{t}, \mathrm{t}^{2} /-18+4.5\right)$ | Dependent curve (AKA definition curve). |
| Curve c | $(9, \mathrm{t})$ | Abscissa definition $(\sqrt[1]{9})$. |
| Curve d | $\left(\mathrm{t}, \mathrm{t}^{1} /-2+4.5\right)$ | $(-)$ solution curve |
| Curve e | $\left(\mathrm{t}, \mathrm{t}^{1} / 2-9 / 2\right)$ | $(+)$ solution curve |
| Crate\| |  |  |

Created with GeoGebra

## Parametric geometry construction for $(\sqrt[1]{9})$.

 odd indices:$(-)$ solution ( $d$ ) comes from $Q 2$ infinity. Passes through $\mathbf{N}$ pole and finds $(\sqrt[1]{9})$ on accretion domain of $\left(M_{1}\right)$.
$(+)$ solution curve $(e)$ comes from $Q 3$ infinity. Passes through $\mathbf{S}$ pole and finds $(\sqrt[1]{9})$ on accretion domain of $\left(M_{1}\right)$.

Parametric geometry construction for $(\sqrt[0]{9})$. ALEXANDER


Figure 4: parametric geometry $(\sqrt[0]{9})$

| Name | Value | Caption |
| :--- | :--- | :--- |
| Curve a | $(4.5 \cos (\mathrm{t}), 4.5 \sin (\mathrm{t}))$ | Independent curve (AKA discovery curve). |
| Curve b | $\left(\mathrm{t}, \mathrm{t}^{2} /-18+4.5\right)$ | Dependent curve (AKA definition curve). |
|  |  | (parametric $\sqrt[0]{9})$. Rest energy of Central Force <br> Field. Limits range of Surface Acceleration on Curve <br> (a), home to Galileo's Incline Plane Kinematics and <br> latus rectum solution curve $\left(9^{\frac{1}{2}}\right)$. |
| Curve j | $\left(\mathrm{t}, \mathrm{t}^{\mathrm{o}} /-2+9 / 2\right)$ |  |

Readings from the Sand Box

| Curve i | $\left(\mathrm{t}, \mathrm{t}^{1} /-2+9 / 2\right)$ | curved space registration: Parametric $\sqrt[1]{9}$ with Central Force Spin. |
| :---: | :---: | :---: |
| Curve f | $\left(\mathrm{t}, \mathrm{t}^{2} /-2+9 / 2\right)$ | $(-)$ solution curve. (parametric $\sqrt[2]{9}$ ) |
| Curve c | (1/9, t) | Curvature value displacement ( $r=9$ ). |
| Curve e |  | Best fit parabola linking Sir Isaac Newton's displacement radius (9) with curvature value ( $\frac{1}{9}$ ) in potential. <br> (inverse square connection) |
| Curve h |  | Best fit parabola connecting Curved Space Mechanical Potential as motive energy on the period time curve (b). $\left(9^{2} \leftrightarrow 9^{\frac{1}{2}}\right)$ |
| Point B | $B=(1,4)$ | (domain1, range4) +endpoint $\left(9^{\frac{1}{2}}\right)$ solution curve latus rectum. Joins: $(\sqrt[0]{9}),(\sqrt[1]{9}),(\sqrt[2]{9})$ |
| Point C | $C=(3,4)$ | (domain $\sqrt[2]{9}$, range 4 ). Intercept of $(\sqrt[0]{9})$ with period time curve $(b) @(\sqrt[2]{9}, 4)$ |
| Point D | $\mathrm{D}=(3,3)$ | Galileo's S\&T1, our first spacetime square. Coordinates of ( $D$ ) map 3seconds Earth Uniform Acceleration field with: ( $3^{2}$ spacetime tiles). <br> One tile of spacetime Earth: $(16 f t ., 1 s)$. <br> Freefall spacetime: $(9 s *(16 f)=144 f t d r o p)$. <br> Terminal velocity: $(6 s *(16 f t)=96 f t / s)$. |

## Created with GeoGebra

Each tile has 1s range and 16ft domain/second/tile.

Solution curves; odd indices and even indices

- Travel from Q2 and Q3 infinity, polar flat line, and intersect abscissa ID.
- Red curves negative and blue positive. Sign curve with slope of +domain abscissa ID intercept.
- index(0) radicand(9): $\left(9^{\frac{1}{0}}\right)$
- There is no domain, only (+/-) range solution curves as rest energy. For a central force to work, index solution curves of a CF field must pass through spin vertices making index(0) solution curves, rest energy of a CF field. $\mathbf{F}$ recognizes a radicand integer in space as displacement using index(1) solution curve to connect Sir Isaac Newton's displacement space ( $r$ ) with CF spin. The solution curves(index 0,1 ,and 2 of radicand 9 ) working this construction, represent the study of Earths Uniform Acceleration Field, Galileo's S\&T1, our $1^{\text {st }}$ spacetime square. Index(0) of any radicand always has latus rectum of index(2) solution curve( f$)$; the ( $\sqrt[2]{\text { displacement }})$. The Uniform Acceleration event(s) happening in this construction, index (0) of radicand(9), is 3 s of freefall.
- Crossover triangle (BCD) Coordinates. (With respect to CF Earth)
- POINT(B): two significant events. Event(1), Unification. All 3 solution curves, (index 0,1 , and 2 ) meet at ( $B$ ), the + LR endpoint for index (2) solution Curve( $f$ ).

These 3 indices, (index 0,1 , and 2), are the only curves needed to construct and analyze CF field intensity.

- Event(2): Quantifies (1 1 $^{\text {st }}$ second) spacetime tile of Galileo's S\&T1; Uniform Acceleration Earth with 1s Central Force range and $16 \mathrm{ft} / \mathrm{sec} / \mathrm{tile}$ as CF domain.
- Point (B, and D): Hypotenuse (BD) of CROSSOVER curve lies on (index (1)) solution curve $(i)$. Leg (BC) of crossover, connects $1^{\text {st }}$ sec tile experience with events on period time curve (b), point( $C$ ). Leg
$(C D)$ : points $(C)$ and $(D)$ share same abscissa ID, $(\sqrt[2]{9})$ or domain integer(3). The coordinates of (B,C,\&D):

$$
B:(1, \sqrt[0]{9}), C:(\sqrt[2]{9}, \sqrt[0]{9}), D:(\sqrt[2]{9}, 3)
$$

After poster for MAA, I standardized protocol constructing indexed solution curves on the $1^{\text {st }}$ ten integers as displacement radii. Principal change is for CrossOver Triangle ( $A, B, C$ ).

INTEGER(9) square space; RADICAND(9) curved space.

Displacement radius(9) is perfect. Crossover pt.(A) just catches Galileo $1^{\text {st }}$ spacetime tile for our first Euclidean SpaceTime Square.

Frame is 3 s long. Drop is $\left(3^{2} * 16\right)$ or 144 ft . Terminal v is $\left(1^{\text {st }}\right.$ derivative of $\left.3^{2}\right)$ or 6*16 for 96ft/s.
(A): $\quad(1, \sqrt[0]{9})$.
(B): $\quad(\sqrt[2]{9}, \sqrt[0]{9})$.
(C):
$(\sqrt[2]{9}, 3)$
Rt. $\Delta$ (ABC): $\quad$ base $(\sqrt{9}-1)$ alt.: $\quad(4-(3))$
Hyp: $\quad\{c \rightarrow \sqrt{5}\}$
Area:
1

The Beatles nailed it. Number(9), number(9), number(9)...
I say integer 9 is our registration with curved space ME. This number is source for both Euclid's $1^{\text {st }}$ spacetime frame and rules of Nature found by Galileo's incline plane researching S\&T1 providing domain and range of Euclid's space time tiles for our Earth $(16 f t, 1 s)$.

It's here and only here that the +latus rectum on curve (f), ( $\sqrt[2]{9}$ ), links these solution curves, $(\sqrt[0]{9}),(\sqrt[1]{9})$, and $(\sqrt[2]{9})$ with counting integer $(9)$ of our square space domain. It's the only CSDA ME construction to link $(\sqrt[1]{9})$ and integer(9) with (3)seconds of Galileo's S\&T1 providing (9) perfect tiles connecting our Earth with God's Creation. (maybe a Jovian $1^{\text {st }}$ spacetime tile provides other parametrics). the hypotenuse ( $A C$ ), found on index(1) solution curve, fits a perfect Euclidean SpaceTime Frame, $1^{\text {st }}$ second tile and most remote corner of frame with nine square tiles. It never happens again on our square space number line.

I use Euclidean Geometry with respect to the tools Galileo had at the time.


Figure 5: Our 1st spacetime frame. Galileo's discovery of Uniform Acceleration for Earth. Tile(1);
$(16 f t, 1 s)$. Displacement integer(9) has $\left(3 s^{2}\right)$ tiles to sum frame with nine tiles., each tile has range of 1 s and domain of ( $16 \mathrm{ft} /$ second/tile).

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Using computer parametric geometry code to construct the focus of an Apollonian parabola section within a right cone.

"It is remarkable that the directrix does not appear at all in Apollonius great treatise on conics. The focal properties of the central conics are given by Apollonius, but the foci are obtained in a different way, without any reference to the directrix; the focus of the parabola does not appear at all... Sir Thomas Heath: "A HISTORY OF GREEK MATHEMATICS" page 119, book II.

Utility of a Unit Circle and Construct Function Unit Parabola may not be used without written permission of my publishing company Sand Box Geometry LLC Alexander, CEO and copyright owner. alexander@sandboxgeometry.com

The computer is my sandbox, the unit circle my compass, and the focal radius of the unit parabola my straight edge. Armed with these as weapon and shield, I go hunting Curved Space Parametric Geometry.

## ALEXANDER; CEO SAND BOX GEOMETRY LLC

## CAGE FREE THINKIN' FROM THE SAND BOX

The square space hypotenuse of Pythagoras is the secant connecting ( $\pi / 2$ ) spin radius $(0,1)$ with accretion point $(2,0)$. I will use the curved space hypotenuse, also connecting spin radius ( $\pi / 2$ ) with accretion point $(2,0)$, to analyze $G$-field mechanical energy curves.


CSDA demonstration of a curved space hypotenuse and a square space hypotenuse together.

We have two curved space hypotenuses because the gravity field is a symmetrical central force and will have an energy curve at the $\mathbf{N}$ pole and one at the $\mathbf{S}$ pole of spin: just as a bar magnet. When exploring changing acceleration energy curves of $\mathrm{M}_{2}$ orbits, we will use the N curve as our planet group approaches high energy perihelion on the north time/energy curve.

The foundation of human mathematics is geometry. If one would take some time to look at the written works (they happen to be library available) of Newton, Kepler, and the time-tested Conic Treatise of Apollonius, you will be face-to-face with the stick art of human mathematics. However, unlike art, freedom of interpretation is not invited. Only a single path of rigorous logic leading to an irrefutable conclusion is proffered. Proofing still rules today, as the only way to structure an argument advancing human math to the next level.

For me, it is not important to understand the proofing used with exploratory Philosophical Geometry of the Masters for this can be as difficult to fathom as a triple integral proof, simply witness the incisive descriptive language, explaining methods used by these great geometers of our past, Huygens, Newton, and Kepler, to name a few, as they ponder Questions of Natural Phenomena of Being using descriptive mathematical relations between lines and curves with the unique irrefutable perspective of picture perfect Classic Geometry. Geometry after-all, is one tongue spoken, written, and understood by all humans.

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